

## Nanoscale domain engineering in SrRuO<sub>3</sub> thin films

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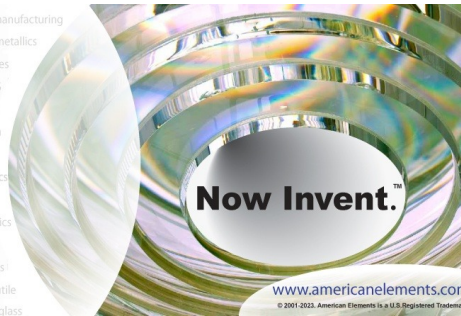


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## ABSTRACT

We investigate nanoscale domain engineering via epitaxial coupling in a set of SrRuO<sub>3</sub>/PbTiO<sub>3</sub>/SrRuO<sub>3</sub> heterostructures epitaxially grown on (110)<sub>o</sub>-oriented DyScO<sub>3</sub> substrates. The SrRuO<sub>3</sub> layer thickness is kept at 55 unit cells, whereas the PbTiO<sub>3</sub> layer is grown to thicknesses of 23, 45, and 90 unit cells. Through a combination of atomic force microscopy, x-ray diffraction, and high resolution scanning transmission electron microscopy studies, we find that above a certain critical thickness of the ferroelectric layer, the large structural distortions associated with the ferroelastic domains propagate through the top SrRuO<sub>3</sub> layer, locally modifying the orientation of the orthorhombic SrRuO<sub>3</sub> and creating a modulated structure that extends beyond the ferroelectric layer boundaries.

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## I. INTRODUCTION

Ferroelectric polarization can be used to affect the properties of other materials. This is well known in ferroelectric field-effect transistors, for example, where the polarization surface charge of the ferroelectric film is used to reversibly dope the adjacent layer, as demonstrated in epitaxial oxide thin film heterostructures.<sup>1</sup>

In this work, a PbTiO<sub>3</sub> layer is sandwiched between two SrRuO<sub>3</sub> layers. In bulk, SrRuO<sub>3</sub> is a ferromagnetic metallic transition-metal oxide and is often used as an electrode in the ferroelectric oxides community.<sup>2</sup> It is also an itinerant ferromagnet with a Curie temperature  $T_C = 160$  K.<sup>3</sup> In thin films of this material, the formation of complex spin textures can be induced by the ferroelectric polarization in an adjacent ferroelectric layer. These include the ferroelectric proximity effect near the BaTiO<sub>3</sub>/SrRuO<sub>3</sub> interface giving rise to an emergent Dzyaloshinskii–Moriya interaction, thereby creating robust magnetic skyrmions.<sup>4</sup> Most recently, in SrRuO<sub>3</sub>/PbTiO<sub>3</sub> heterostructures, a ferroelectrically induced magnetic spin crystal was observed.<sup>5</sup>

SrRuO<sub>3</sub> is not only affected by the polarization in adjacent layers but also by the epitaxial strain imposed by the substrate.<sup>6,7</sup> When grown on SrTiO<sub>3</sub>, epitaxial SrRuO<sub>3</sub> layers are organized into structural domains, according to six possible orientations of the

orthorhombic unit cell with respect to the cubic substrate. The orientation of the orthorhombic unit cell and resulting domain structure are affected by the steps and terraces at the surface of the SrTiO<sub>3</sub> substrate.<sup>8</sup> The growth of SrRuO<sub>3</sub> onto the vicinal planes of miscut SrTiO<sub>3</sub> substrates leads to the privileged development of a majority single domain orientation in which small domains with different orientations are embedded.<sup>9</sup> In addition, control of the SrRuO<sub>3</sub> can be achieved not only through the choice of substrate<sup>10</sup> but also by modifying the growth temperature.<sup>11</sup> Further structural domain engineering has been conducted through control of substrate miscut direction, demonstrating a one-to-one correspondence between structural domains and magnetic domains.<sup>12</sup>

A structural coupling can also be achieved by strain propagation between the different layers themselves. As was shown in PbTiO<sub>3</sub>/SrTiO<sub>3</sub>/PbTiO<sub>3</sub> heterostructures on GdScO<sub>3</sub>, where the structural coupling between the PbTiO<sub>3</sub> and SrTiO<sub>3</sub> layers resulted in periodic polar waves in the SrTiO<sub>3</sub>,<sup>13</sup> in SrRuO<sub>3</sub>/PbTiO<sub>3</sub> superlattices, the large local deformations of the ferroelectric lattice are accommodated by periodic lattice modulations of the metallic SrRuO<sub>3</sub> layers with very large curvatures.<sup>14</sup>

At the core of the heterostructure studied here is PbTiO<sub>3</sub>, a tetragonal ferroelectric with a polarization developing along the *c*-axis mostly due to ionic displacements. In PbTiO<sub>3</sub> thin films,

the orientation of the polarization and arrangement into domain structures have been theoretically studied,<sup>15–20</sup> and are described by phase diagrams with regions of different domain configurations as a function of epitaxial strain and temperature (see review by Schlom *et al.*<sup>21</sup>). The domain pattern is also affected by the film thickness<sup>22</sup> and electrostatic boundary conditions.<sup>23,24</sup> Complex polarization configurations in PbTiO<sub>3</sub> have recently been reported in PbTiO<sub>3</sub>/SrTiO<sub>3</sub> superlattices,<sup>14,25–30</sup> with simultaneous control of these configurations using electric fields and light, giving rise to novel phenomena such as negative capacitance.<sup>31</sup> When grown on DyScO<sub>3</sub>, PbTiO<sub>3</sub> takes the *a/c* phase, where the polarization forms ordered ferroelastic domains (*a/c* twins), resulting in distortions of the film surface visible by atomic force microscopy (AFM).<sup>32–35</sup>

Whether through ferroelectric polarization or strain effects, controlling the structure and morphology of the SrRuO<sub>3</sub> thin films is of importance as it will affect the film electronic resistivity via structural and electronic coupling. Here, we study the structural coupling between oxide thin film layers on a set of SrRuO<sub>3</sub>/PbTiO<sub>3</sub>/SrRuO<sub>3</sub> heterostructures epitaxially grown on (110)<sub>o</sub>-oriented DyScO<sub>3</sub> substrates. We establish the direct role that the ferroelastic domain structure in PbTiO<sub>3</sub> plays in the determination of the orthorhombic domain structure in SrRuO<sub>3</sub>.

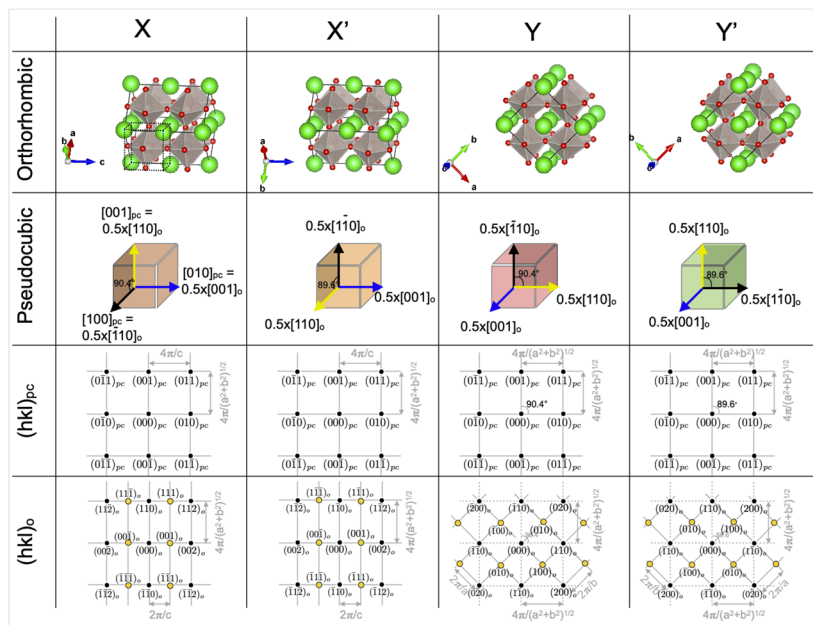
## II. RESULTS

A series of samples was grown by off-axis radio-frequency (RF) magnetron sputtering on (110)<sub>o</sub>-oriented DyScO<sub>3</sub> substrates, with

the bottom and top SrRuO<sub>3</sub> electrodes of 55 unit cells (u.c.) and a PbTiO<sub>3</sub> film thickness of 23, 45, and 90 u.c. (see Sec. IV A for details of sample growth).

The substrate, DyScO<sub>3</sub>, is orthorhombic with room temperature lattice parameters (in the *Pbnm* space group)  $a_o = 5.443(2)$  Å,  $b_o = 5.717(2)$  Å, and  $c_o = 7.901(2)$  Å.<sup>36</sup> It is often useful to also refer to the pseudocubic unit cell, where the lattice parameters can be calculated as  $a_{pc} = c_{pc} = \frac{\sqrt{a_o^2 + b_o^2}}{2} = 3.947$  Å,  $b_{pc} = c_o/2 = 3.951$  Å,  $\alpha_{pc} = \gamma_{pc} = 90^\circ$ , and  $\beta_{pc} = 2 \cdot \arctan(a_o/b_o) = 87.187^\circ$  at room temperature. Here, “*pc*” subscript refers to the pseudocubic unit cell, while “*o*” is used to refer to the orthorhombic unit cell. For (110)<sub>o</sub>-oriented DyScO<sub>3</sub>, the out-of-plane [001]<sub>pc</sub> direction is equivalent to [110]<sub>o</sub>, while the in-plane directions [100]<sub>pc</sub> and [010]<sub>pc</sub> are equivalent to [110]<sub>o</sub> and [001]<sub>o</sub>, respectively (see the supplementary material, Fig. S1).

The bottom and top electrodes, SrRuO<sub>3</sub>, are orthorhombic with bulk room temperature lattice parameters (in the *Pbnm* space group)  $a_o = 5.57$  Å,  $b_o = 5.53$  Å, and  $c_o = 7.85$  Å,<sup>37</sup> corresponding to the pseudocubic unit cell parameters  $a_{pc} = c_{pc} = 3.924$  Å,  $b_{pc} = 3.925$  Å,  $\alpha_{pc} = \gamma_{pc} = 90^\circ$ , and  $\beta_{pc} = 90.413^\circ$ . According to the Glazer notation, octahedral tilting in orthorhombic SrRuO<sub>3</sub> is described by  $a^- a^- c^+$ , implying that RuO<sub>6</sub> octahedra are rotated in opposite directions by equivalent magnitude along [100]<sub>pc</sub> and [010]<sub>pc</sub> (out-of-phase) and in the same direction about [001]<sub>pc</sub> (in-phase).<sup>38,39</sup> On (110)<sub>o</sub>-oriented DyScO<sub>3</sub> substrate, SrRuO<sub>3</sub> can grow with different possible orientations,<sup>8,12</sup> as described in Fig. 1, and supplementary material, Figs. S1 and S2.



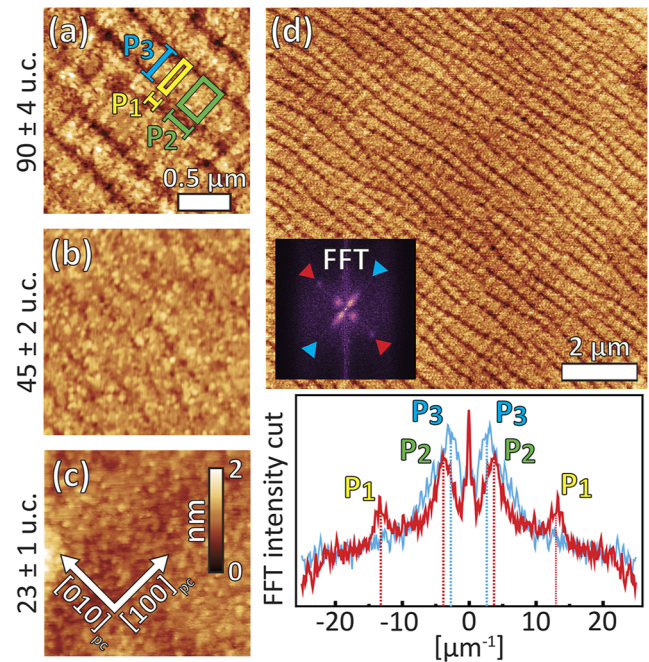
**FIG. 1.** Detailed representation of four of the possible orthorhombic orientations of the SrRuO<sub>3</sub> on the (110)<sub>o</sub>-oriented DyScO<sub>3</sub> substrate (in the *Pbnm* space group). Each column corresponds to a different orientation: X, X', Y, and Y'. First row: perspective view, with arrows  $\vec{a} \parallel [100]_o$ ,  $\vec{b} \parallel [010]_o$  and  $\vec{c} \parallel [001]_o$  corresponding to the axis of the orthorhombic unit cell. Second row: corresponding pseudocubic representation. Third row: reciprocal space representation and (hkl) indices corresponding to the pseudocubic structure. Fourth row: reciprocal space representation and (hkl) indices corresponding to the orthorhombic structure, highlighting the position of the “half-order” peaks. The six possible orthorhombic orientations can be found in supplementary material, Figs S1 and S2.

Last, the  $\text{PbTiO}_3$  is ferroelectric below a bulk critical temperature of 765 K with a tetragonal structure and lattice parameters  $a = b = 3.904 \text{ \AA}$  and  $c = 4.152 \text{ \AA}$  at room temperature. The in-plane strain imposed by  $\text{DyScO}_3$  on  $\text{PbTiO}_3$  films can thus be calculated as  $\frac{a_{pc}-a_0}{a_{pc}} = -0.25\%$  along  $a_{pc}$  and  $\frac{b_{pc}-a_0}{b_{pc}} = -0.16\%$  along  $b_{pc}$ , where  $a_0$  is the extrapolated lattice parameter of  $\text{PbTiO}_3$  in the room-temperature cubic paraelectric phase,  $a_0 = 3.957 \text{ \AA}$  for  $\text{PbTiO}_3$ . To accommodate this strain,<sup>40</sup>  $\text{PbTiO}_3$  thin films on  $\text{DyScO}_3$  at room temperature are expected to be in the  $a/c$ -phase, with regions where the  $c$ -axis points out-of-plane ( $c$ -domains) as well as regions where it points in-plane ( $a$ -domains), giving rise to a ferroelastic  $a/c$ -domain configuration with  $90^\circ$  domain walls. The latter are parallel to the  $\{101\}_{pc}$  crystallographic planes and, thus, are inclined at about  $45^\circ$  with respect to the film/substrate interface, as predicted in Ref. 17 and demonstrated experimentally (see, for example, Refs. 33, 34, and 41). In addition to these ferroelastic domains, the electrostatic boundary conditions and depolarization field arising from an incomplete screening of the surface bound charges can lead the  $c$ -domains to alternate between “up” ( $c^+$ ) and “down” ( $c^-$ ) orientations. Although the surface bound charges of our  $\text{PbTiO}_3$  films are screened by the top and bottom  $\text{SrRuO}_3$  electrodes, this screening is incomplete<sup>42–46</sup> and the depolarization field still plays a role. Such a combination of mechanical and electrostatic constraints can then result in flux-closure structures, as observed in strained  $\text{PbTiO}_3$  thin films.<sup>35,45,47,48</sup>

### A. Topographic modulation observed at the heterostructure surface using atomic force microscopy

Figure 2(a) shows atomic force microscopy (AFM) images for the three  $\text{SrRuO}_3/\text{PbTiO}_3/\text{SrRuO}_3$  heterostructures grown on  $\text{DyScO}_3$ . The AFM topography images reveal that as the  $\text{PbTiO}_3$  layer thickness increases, trenches develop at the surface of the  $\text{SrRuO}_3$  top layer in an organized pattern. For the samples with 23 and 45 u.c. thick  $\text{PbTiO}_3$  layers, this pattern is hardly visible, and the top  $\text{SrRuO}_3$  is smooth. The pattern gets more pronounced and anisotropic with increasing  $\text{PbTiO}_3$  layer thickness, with long and deep trenches parallel to the  $\text{DyScO}_3$   $[001]_o$  axis, and smaller trenches parallel to the  $\text{DyScO}_3$   $[\bar{1}10]_o$  axis, while the surface roughness stays reasonably low [root mean square (rms) roughness values ranging from 157 to 393 pm over surfaces of  $10 \times 10 \mu\text{m}^2$ ].

The pattern that we observe at the surface of the  $\text{SrRuO}_3$  top layer is comparable to what has been seen in  $\text{PbTiO}_3$  layers grown on  $\text{DyScO}_3$  substrates in Ref. 34, attributed to the presence of periodic ferroelastic  $a/c$  domains. To extract the period of the distortions visible on the surface of the samples, we calculate the fast Fourier transform (FFT) of the autocorrelation image, as shown in Fig. 2(d) for the sample with the 90 u.c. thick  $\text{PbTiO}_3$  layer. Along  $\text{DyScO}_3$   $[001]_o$  (red), two periods are visible,  $P_1 = 77 \pm 1 \text{ nm}$  and  $P_2 = 280 \pm 3 \text{ nm}$ , while along  $\text{DyScO}_3$   $[\bar{1}10]_o$  (blue), a unique period  $P_3 = 335 \pm 4 \text{ nm}$  is visible. These periods have been illustrated on the topography image of the corresponding sample as yellow (with dimensions  $P_1 \times P_3$ ) and green (with dimensions  $P_2 \times P_3$ ) rectangles. All these values are reported in Table S1 (supplementary material).

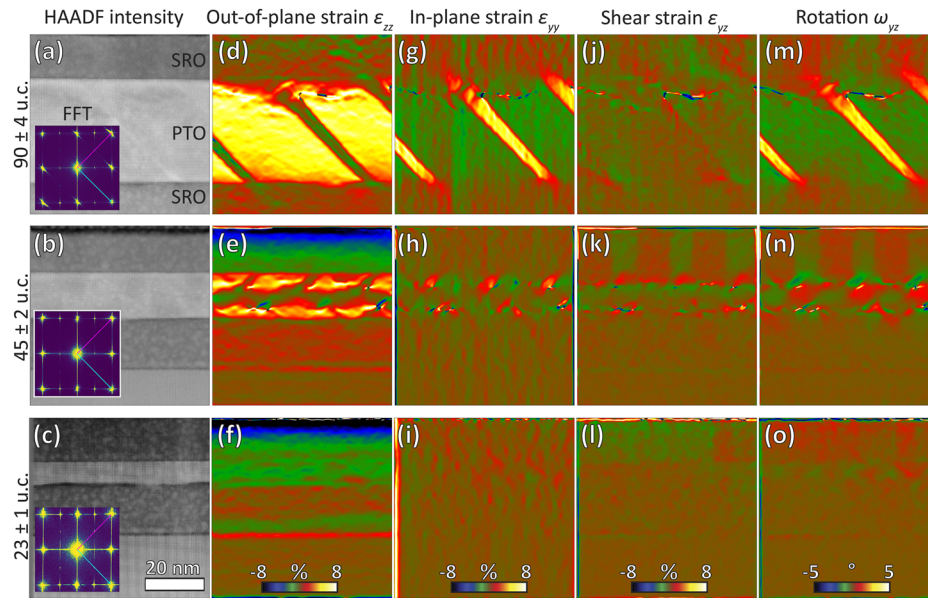


**FIG. 2.** AFM topography images obtained on the different samples. The color scale varies between 0 and 2 nm. The sample orientation was fixed with respect to the substrate pseudocubic axis  $[100]_{pc}/\text{DyScO}_3$   $[\bar{1}10]_o$  and  $[010]_{pc}/\text{DyScO}_3$   $[001]_o$ . (a)–(c)  $2 \times 2 \mu\text{m}^2$  scans for the three samples: (a)  $90 \pm 4$  u.c., (b)  $45 \pm 2$  u.c. and (c)  $23 \pm 1$  u.c. thick  $\text{PbTiO}_3$  between top and bottom  $\text{SrRuO}_3$  electrodes ( $55 \pm 2$  u.c. thick) on  $\text{DyScO}_3$  substrates, showing that as the  $\text{PbTiO}_3$  layer thickness increases, trenches develop at the surface of the  $\text{SrRuO}_3$  top layer. (d) A larger  $10 \times 10 \mu\text{m}^2$  scan for the 90 u.c. thick  $\text{PbTiO}_3$  sample displays the anisotropic pattern, with long and deep trenches parallel to the  $[010]_{pc}$  axis, and smaller trenches parallel to the  $[100]_{pc}$  axis. In the image obtained from the fast Fourier transform of the topography measurement (inset), periodic peaks along  $[100]_{pc}$  and  $[010]_{pc}$  are visible (see cuts), allowing us to determine the periods. Along  $[010]_{pc}$  (red), two periods are visible,  $P_1 = 77 \pm 1 \text{ nm}$  and  $P_2 = 280 \pm 3 \text{ nm}$ , while along  $[100]_{pc}$  (blue), a unique period  $P_3 = 335 \pm 4 \text{ nm}$  is visible. These sizes have been drawn on the topography image (a) of the corresponding sample as yellow and green rectangles.

### B. Domain structures observed by scanning transmission electron microscopy

To better understand the origin of this pattern visible at the surface of the  $\text{SrRuO}_3$  top layer, we turned to cross-sectional scanning transmission electron microscopy (STEM) images. The three samples were cut and prepared for STEM measurements to obtain slices in the plane defined by the  $[001]_o$  (horizontal direction) and  $[110]_o$  (vertical direction) axes of  $\text{DyScO}_3$ . STEM images were obtained using bright field (BF), annular bright field (ABF), medium angle annular dark field (MAADF) and high-angle annular dark field (HAADF) detectors along the  $\text{DyScO}_3$   $[\bar{1}10]_o$  zone-axis (see Sec. IV C for more technical details).

The domain walls in the  $\text{PbTiO}_3$  layers can be directly seen in the STEM images, as shown in Fig. 3 [(a)–(c) - HAADF images] and in Fig. 6 [(a)–(c) - BF images], while the  $\text{SrRuO}_3$  layers appear rather homogeneous. The  $\text{PbTiO}_3$  layers in the three samples studied have different domain configurations, where the expected  $a/c$



**FIG. 3.** HAADF images and strain maps for the three samples: (top row)  $90 \pm 4$  u.c., (center row)  $45 \pm 2$  u.c., and (bottom row)  $23 \pm 1$  u.c. thick  $\text{PbTiO}_3$  between top and bottom  $\text{SrRuO}_3$  electrodes ( $55 \pm 2$  u.c. thick) on  $\text{DyScO}_3$  substrates. (a)–(c) HAADF images, with the inset showing the FFT and the two vectors used for the GPA analysis indicated by the blue and purple arrows. (d)–(f) Out-of-plane strain  $\epsilon_{zz}$ . (g)–(i) In-plane strain  $\epsilon_{yy}$ . (j)–(l) Shear strain  $\epsilon_{yz}$ . (m)–(o) Rotation  $\omega_{yz}$ . The strain and rotation values are calculated with respect to a reference lattice here chosen as the substrate. The same intensity scales from  $-8\%$  to  $8\%$  (strain) and from  $-5^\circ$  to  $5^\circ$  (rotation) are used for the three samples to allow for comparison. Different contrasts are observed in the  $\text{PbTiO}_3$  layers, corresponding to the different ferroelastic domain configurations, from  $a/c$  for the thickest to flux-closure for the thinner one. The images interestingly reveal an additional contrast appearing only in the top  $\text{SrRuO}_3$  layers, for the samples with the 45 u.c. and the 90 u.c. thick  $\text{PbTiO}_3$  layers, and propagating all the way to the top surface.

pattern for the thicker  $\text{PbTiO}_3$  layer transforms into a flux-closure pattern for the thinner  $\text{PbTiO}_3$  layers [see Ref. 35 for a complete x-ray diffraction (XRD) based investigation of ferroelectric domain configuration in an extended series of samples].

### 1. Geometric phase analysis

To study the local strain induced by these different domain configurations, we turn to Geometric Phase Analysis (GPA).<sup>49</sup> This is done by taking the FFT of the HAADF-STEM images in Fig. 3, selecting two peaks [here  $(01\bar{1})_{pc}$  and  $(011)_{pc}$ ] corresponding to two reciprocal lattice vectors defining the lattice, and getting the inverse Fourier transform containing information about local displacements of the atomic planes along these two vectors. The local strain components are calculated from the derivative of the obtained displacement field: in-plane strain  $\epsilon_{yy}$  (along  $\text{DyScO}_3[001]_o$ ), out-of-plane strain  $\epsilon_{zz}$  (along  $\text{DyScO}_3[110]_o$ ), shear strain  $\epsilon_{yz}$  and rotation  $\omega_{yz}$ .

Looking first at the results within the  $\text{PbTiO}_3$  layers, we see from the HAADF images and from the GPA maps that the domain patterns vary with  $\text{PbTiO}_3$  thickness. For the 90 u.c. thick  $\text{PbTiO}_3$  in Fig. 3 (top row), we see large regions with a high out-of-plane strain but low in-plane strain, shear and rotation, corresponding to  $c$ -domains, i.e., regions where the polarization is out-of-plane. These regions are separated by narrower features, with high in-plane strain, and rotation, but low out-of-plane strain and shear, corresponding to  $a$ -domains, i.e., regions where the polarization is in-plane. These results confirm a typical well developed  $a/c$ -phase. For the 45 u.c. thick  $\text{PbTiO}_3$  layer in Fig. 3 (center row), the strain

map is more complex, with alternating regions with large out-of-plane strain or large in-plane strain close to each interface, and reduced strain at the center of the  $\text{PbTiO}_3$  layer, clearly different from an  $a/c$ -phase (see the supplementary material, Fig. S4). This pattern is more comparable to the flux closure configuration observed for  $\text{PbTiO}_3$  with similar thickness grown without electrodes.<sup>47</sup> Finally, for the 23 u.c. thick  $\text{PbTiO}_3$  layer in Fig. 3 (bottom row), the  $\text{PbTiO}_3$  strain maps are more homogeneous compared to the results obtained for the two other samples. This indicates that for this sample, the distortions related to the ferroelectric/ferroelastic domain configuration in the  $\text{PbTiO}_3$  layer are small with respect to the homogeneous strain induced by the substrate. The most pronounced contrast is visible in the rotation map and corresponds to a pattern with a period of  $\sim 16$  nm, in agreement with the value found by XRD (see the supplementary material, Fig. S3 and Table S1 for comparison).

Concentrating now on the  $\text{SrRuO}_3$  layers, we see that the bottom ones are predominantly homogeneous in all three samples. However, this is not the case for the top  $\text{SrRuO}_3$  layers, where different contrasts appear for the three different  $\text{PbTiO}_3$  thicknesses. While the  $\text{SrRuO}_3$  layer on top of the 23 u.c.  $\text{PbTiO}_3$  looks rather homogeneous, regions with different shear strain and rotation values alternate in the  $\text{SrRuO}_3$  layers grown on top of the 45 and 90 u.c.  $\text{PbTiO}_3$  with boundaries propagating along the  $[001]_{pc}$  growth direction.

For the sample with 90 u.c.  $\text{PbTiO}_3$ , at the interface with each  $a$ -domain and above the obtuse angle formed by the  $a/c$  domain

wall, the rotation is positive (red), while it is negative (green) above the acute angle [Fig. 3(m)]. The rotation then propagates directly to the top surface along the growth direction. A similar modulation of the rotation is also observed in the SrRuO<sub>3</sub> bottom electrode, with positive rotation below the obtuse angle of the *a/c* domain wall, and negative rotation below the acute angle. However, for the bottom electrode, this modulation is limited to the vicinity of the interface and does not propagate through the whole SrRuO<sub>3</sub> bottom electrode thickness, most likely due to substrate clamping.

For the sample with 45 u.c. PbTiO<sub>3</sub>, regions with a positive rotation (red) alternate with regions with a negative rotation (green) [Fig. 3(n)], with a reduced rotation amplitude compared to the sample with 90 u.c. thick PbTiO<sub>3</sub>, but with sharper boundaries. The period of this pattern follows the period of the ferroelectric domains underneath.

## 2. Discriminating between $X/X'$ and $Y/Y'$ using fast Fourier transforms

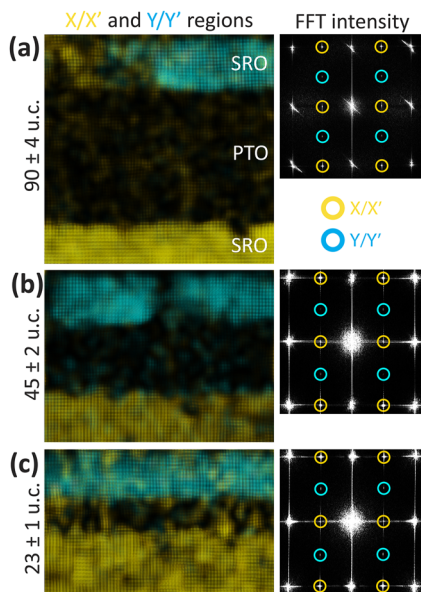
To better understand the origin of this contrast, one can use the FFT and deduce the orientation of the SrRuO<sub>3</sub> layers from the obtained Bragg peak positions. In the FFT images in Fig. 4, the bright peaks of the pseudocubic lattice are clearly visible, corresponding to  $\{0\ k\ l\}_{pc}$  planes with *k* and *l* integer indices. In addition to these peaks, weaker peaks also appear at positions corresponding to planes

with half-integer Miller indices  $\{0\ 1/2\ 1/2\}_{pc}$  highlighted in blue and  $\{0\ 1/2\ 1\}_{pc}$  highlighted in yellow. These peaks come from the orthorhombic unit cell, which is composed of four pseudocubic unit cells, as described in Fig. 1. The position of the additional peaks is a clear indication of the orientation of the orthorhombic unit cell. The peaks corresponding to the  $\{0\ 1/2\ 1\}_{pc}$  planes in the FFT appear when the orthorhombic long axis  $[001]_o$  is oriented in-plane, parallel to the  $[010]_{pc}$  axis, and correspond to the  $X$  or  $X'$  orientation (note that it is not possible to discriminate between  $X$  or  $X'$  in this measurement geometry). The peaks corresponding to the  $\{0\ 1/2\ 1/2\}_{pc}$  planes, on the other hand, are the signature of the orthorhombic long axis  $[001]_o$  being oriented in-plane, parallel to the  $[100]_{pc}$  axis, corresponding to  $Y$  or  $Y'$  orientation.

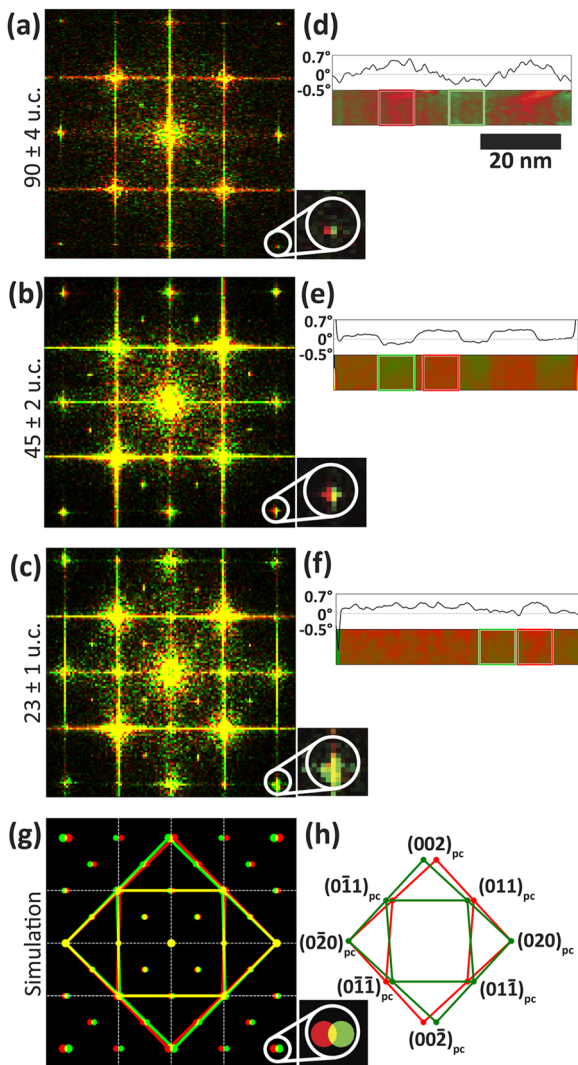
By selecting the different half order peaks and reconstructing the images in Fig. 4, we find that the  $\{0\ 1/2\ 1\}_{pc}$  peaks corresponding to  $X/X'$  orientation originate from the substrate and the bottom SrRuO<sub>3</sub> electrode for all three samples, while the  $\{0\ 1/2\ 1/2\}_{pc}$  peaks corresponding to  $Y/Y'$  originate from the top SrRuO<sub>3</sub> electrode. We also note that for the sample with the thickest PbTiO<sub>3</sub> layer, the top SrRuO<sub>3</sub> shows a mixed  $X/X'$  and  $Y/Y'$  character. Although already highlighting differences in the top SrRuO<sub>3</sub> layers for the different samples, this is not enough yet to explain the contrast observed in the strain and rotation maps in the GPA analysis in the SrRuO<sub>3</sub> top layers for the samples with 45 and 90 u.c. thick PbTiO<sub>3</sub> layers. This will be further investigated below, where we show that it is possible to discriminate between  $Y$  and  $Y'$ .<sup>50</sup>

## 3. Discriminating between $Y$ and $Y'$ using fast Fourier transforms

FFT was performed locally on selected regions corresponding to different shear strain and rotation values in the top SrRuO<sub>3</sub> layers of the three samples, as shown in Fig. 5. The regions of interest are selected based on the largest contrast in the GPA rotation maps in Figs. 5(d)–5(f), and give the colored diffraction patterns in (a)–(c) for the sample with 90 u.c. (a), 45 u.c. (b), and 23 u.c. (c) PbTiO<sub>3</sub>, respectively, combining the FFT Bragg peaks in red and in green for the two regions. For the samples with 90 and 45 u.c. PbTiO<sub>3</sub>, the two diffraction patterns do not overlap perfectly, and a very small horizontal shift can be observed [the  $(022)_{pc}$  peak is enlarged for clarity]. For comparison, the diffraction pattern has been simulated for the  $Y$  and  $Y'$  orientations by arbitrarily increasing the difference between the  $a_o$  and  $b_o$  parameters ( $a_o = 5.62$  and  $b_o = 5.48$  in arbitrary units), making the difference in the Bragg peak positions more visible: the difference between  $Y$  and  $Y'$  results in horizontal shifts of peaks, as measured experimentally. No shift is observed for the SrRuO<sub>3</sub> top electrode above 23 u.c. PbTiO<sub>3</sub>. From this, we can conclude that the contrast seen in the GPA strain and rotation maps for the two samples with the thickest PbTiO<sub>3</sub> layers arises from alternating  $Y$  and  $Y'$  domains. Moreover, Fig. 5(d) shows that the transition from  $Y$  to  $Y'$  domains for the sample with 90 u.c. PbTiO<sub>3</sub> is gradual with a modulation of the rotation following a sinusoidal behavior between  $0.3^\circ$  and  $-0.3^\circ$  with a period of  $\sim 30$  nm. In comparison, this transition is much sharper for the sample with the 45 u.c. PbTiO<sub>3</sub> layer, with the modulation of the rotation following a step-like function between  $0.15^\circ$  and  $-0.2^\circ$  with a period of  $\sim 20$  nm as shown in Fig. 5(e), hinting at the presence of proper twin boundaries between the  $Y$  and  $Y'$  domains. Further discussion and a high resolution



**FIG. 4.** FFT analysis of the SrRuO<sub>3</sub> electrodes orientation in the three samples with (a) 90 u.c., (b) 45 u.c., and (c) 23 u.c. thick PbTiO<sub>3</sub> layers shows the presence of bright peaks corresponding to the pseudocubic lattice at  $\{0\ k\ l\}_{pc}$  with *k* and *l* integer indices, and weaker peaks at half-integer Miller indices  $\{0\ 1/2\ 1\}_{pc}$ , corresponding to  $X/X'$  (highlighted in yellow), and  $\{0\ 1/2\ 1/2\}_{pc}$ , corresponding to  $Y/Y'$  orientation (highlighted in blue). The color maps are obtained by FFT filtering the orthorhombic superstructures, demonstrating the  $X/X'$  orientation for the bottom SrRuO<sub>3</sub> for the three samples, and the  $Y/Y'$ -orientation for the top SrRuO<sub>3</sub> for the two samples with the thinner PbTiO<sub>3</sub> layers (b) and (c) and a mixed  $X/X'$ - $Y/Y'$  for the sample with the thickest PbTiO<sub>3</sub> layer (a).



**FIG. 5.** FFT of  $Y/Y'$  oriented top  $\text{SrRuO}_3$  regions of the samples with (a) 90 u.c.  $\text{PbTiO}_3$  (b) 45 u.c.  $\text{PbTiO}_3$  and (c) 23 u.c.  $\text{PbTiO}_3$  compared to the simulation (g) with  $a_0 = 5.62$  and  $b_0 = 5.48$  parameters (in arbitrary units). The colored diffraction patterns of the top  $\text{SrRuO}_3$  in (a)–(c) combine the FFT Bragg peaks of the  $Y$  domain in red and the  $Y'$  domain in green, where the regions of interest were selected based on the regions of largest contrast in the GPA rotation maps in (d)–(f).

TEM image of such a twin boundary is shown in the supplementary material, Sec. S4.

### III. DISCUSSION

We show that the complex tilt pattern of the  $\text{PbTiO}_3$  layer is responsible for the deformation of the  $\text{SrRuO}_3$  layer deposited on top, resulting in the periodic pattern visible in the topography by

AFM. Our STEM measurements highlight how the domain pattern in the  $\text{PbTiO}_3$  layer affects the strain state and crystal orientation in the  $\text{SrRuO}_3$  top layer, with clear differences for the three samples with different  $\text{PbTiO}_3$  layer thicknesses.

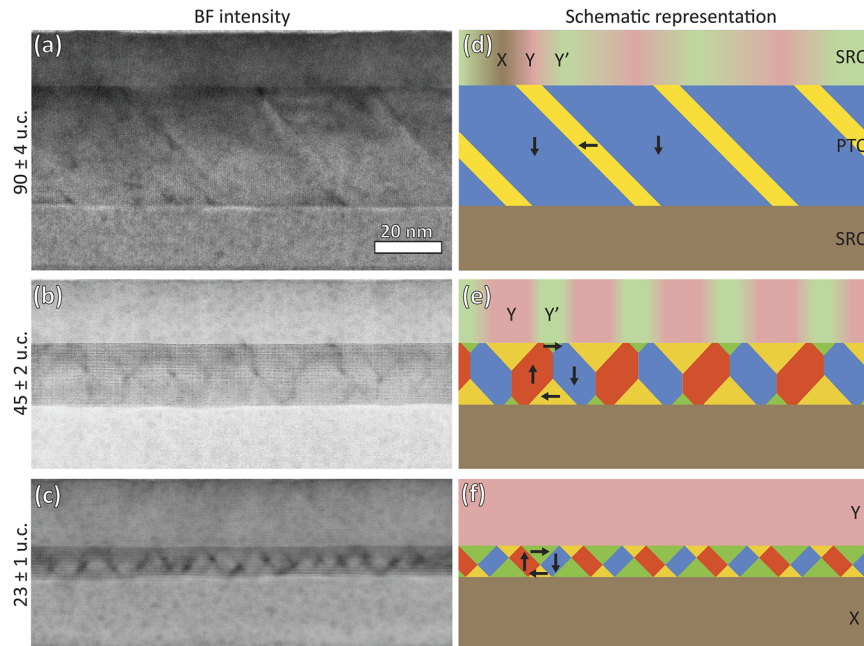
We find that the top  $\text{SrRuO}_3$  layers show a different behavior for each of the three samples, shown in Fig. 6, while the bottom  $\text{SrRuO}_3$  layers systematically have the same orientation as the  $\text{DyScO}_3$  substrate ( $X$ -orthorhombic orientation), probably pinned by the interfacial continuity of the oxygen octahedral rotation imposed by the substrate.

For the sample with a 23 u.c.  $\text{PbTiO}_3$  layer, where no pattern is visible in the topography, we observe a flux-closure type  $\text{PbTiO}_3$  domain structure and correspondingly a null or weakly distorted  $\text{SrRuO}_3$  structure, homogeneously in the  $Y$ -orthorhombic orientation, as shown in Fig. 6 (bottom row).

For the sample with a 45 u.c.  $\text{PbTiO}_3$  layer, where a pattern is only weakly observed in the topography, we again have a flux-closure type  $\text{PbTiO}_3$  domain structure. However, in Fig. 3, if we compare the out-of-plane (e) and in-plane (h) strain maps close to the interfaces, the strain pattern locally resembles that of the  $a/c$  phase [Figs. 3(d) and 3(g)]. This points at a nascent  $a/c$  phase near the top interface, allowing a more pronounced deformation that translates into a clearly distorted  $\text{SrRuO}_3$  structure that shares the same periodicity as the  $\text{PbTiO}_3$ . The top  $\text{SrRuO}_3$  thus alternates between  $Y$ - and  $Y'$ -orthorhombic orientations—with a period corresponding to the period of the domain pattern in  $\text{PbTiO}_3$ . The mechanism that drives the rotation of the top  $\text{SrRuO}_3$  is strain-induced: due to the small shear and rotation in the top layer of  $\text{PbTiO}_3$ , the  $\text{PbTiO}_3$ /top  $\text{SrRuO}_3$  interface is not totally flat (left and right inclination). The formation of  $Y/Y'$  domains is a good way to minimize the interface strain [Fig. 6 (center row)].

Finally, in the sample with the 90 u.c. thick  $\text{PbTiO}_3$  layer, where the topography displays noticeable tilts and trenches, the  $a/c$ -phase is fully developed, with strong  $\text{PbTiO}_3$  lattice heterogeneity that partially imprints on the top  $\text{SrRuO}_3$  electrode. Here, the top  $\text{SrRuO}_3$  exhibits domains with alternating primary  $Y$ - and  $Y'$ -orthorhombic orientations, and some  $X$  interstitial regions. The positive and negative rotation on the  $\text{SrRuO}_3$  correspond to the  $Y$  and  $Y'$  domains, as evidenced by the GPA shear strain and rotation maps. In between these  $Y$  and  $Y'$  domains, a very tiny  $X$ -orientated region is often observed in the FFT. This is typically restrained to a 10 nm width domain at the interface between the  $Y$  and  $Y'$  domains, where no rotation was observed on the GPA map. It is different from the case with the 45 u.c. thick  $\text{PbTiO}_3$  layer, where sharp interfaces and no  $X$  oriented domain were observed between the  $Y$  and  $Y'$  domains.

Our work demonstrates that the large structural distortions associated with ferroelastic domains propagate through the top  $\text{SrRuO}_3$  layer, creating a modulated structure that extends beyond the ferroelectric layer thickness, allowing domain engineering in the top  $\text{SrRuO}_3$  electrode. Since there exists a one-to-one correspondence between the structural and magnetic domains,<sup>12</sup> our approach allows magnetic domain engineering in  $\text{SrRuO}_3$  thin films through structural domain engineering to be realized. This work paves a new path toward control of magnetic domains via structural coupling to ferroelastic domains.



**FIG. 6.** STEM-BF images (a)–(c) on three different samples, together with the sketches (d)–(f) representing the different polarization patterns in the PbTiO<sub>3</sub> layers and the induced crystallographic domains in the top SrRuO<sub>3</sub> layers: (top row) 90±4 u.c., (center row) 45±2 u.c., and (bottom row) 23±1 u.c. thick PbTiO<sub>3</sub> between top and bottom SrRuO<sub>3</sub> electrodes (55±2 u.c. thick) on DyScO<sub>3</sub> substrates. From these images, the domain walls are visible in the PbTiO<sub>3</sub> layers, forming the expected *a/c* pattern for the thicker PbTiO<sub>3</sub> layer and transforming into a flux-closure pattern for the thinner PbTiO<sub>3</sub> layers. In the PbTiO<sub>3</sub> layers, domains with up polarization are shown in red, down in blue, left in yellow, and right in green. In the SrRuO<sub>3</sub> layers, the *X* (or *X'*) orientation is shown in brown, *Y* in red, and *Y'* in green.

## IV. EXPERIMENTAL TECHNIQUES

### A. Sample growth

The three samples were deposited using our in-house constructed off-axis radio-frequency magnetron sputtering system, equipped with three different guns allowing the deposition of heterostructures and solid solutions of high crystalline quality. PbTiO<sub>3</sub> thin films were deposited at 560 °C, in 180 mTorr of a 20:29 O<sub>2</sub>/Ar mixture, at a power of 60 W, and using a Pb<sub>1.1</sub>TiO<sub>3</sub> target with 10% excess Pb to compensate for its volatility. SrRuO<sub>3</sub> layers were deposited from a stoichiometric target in 100 mTorr of an O<sub>2</sub>/Ar mixture of ratio 3:60 at a power of 80 W. The bottom layer was grown at 640 °C, while for the top layer, the temperature was kept at the growth temperature used for PbTiO<sub>3</sub>, i.e., 560 °C, to avoid possible damage of the PbTiO<sub>3</sub> layer. Huettinger PFG 300 RF power supplies are used in power control mode. The sample holder is grounded during deposition, but the sample surface is left floating.

### B. Atomic force microscopy

Topography measurements were performed using a *Digital Instrument Nanoscope Multimode DI4* with a *Nanonis* controller.

### C. Scanning transmission electron microscopy

Cross-sectional slices prepared by a focus ion beam allow the imaging of domain structures by scanning transmission electron

microscopy. Experiments were acquired on Nion Cs-corrected UltraSTEM200 at 100 kV operating voltage. A convergence angle of 30 mrad was used to allow high-resolution atomic imaging with a typical spatial resolution of 1 Å. Three imaging detectors in the STEM are used to simultaneously obtain bright field, annular bright field or medium angle annular dark field, and high angle annular dark field images. For ABF-MAADF imaging, the inner-outer angles can be continuously adjusted between 10–20 and 60–120 mrad. Most ABF images were collected with 15–30 mrad and MAADF images with 40–80 mrad angular ranges.

For the high-resolution HAADF images used to extract GPA, to minimize the influence of the sample drift and environmental noise, a series of fast-scan (low exposure time) HAADF images was taken in the same region; afterward, a script based on Gatan DigitalMicrograph software aligned and summed them together. This technique typically used 20 4k × 4k images with 1 μs exposure time per pixel.

GPA is an algorithm that reconstructs the displacement field  $\vec{u}(\vec{r})$  from HAADF images by measuring the displacement of lattice fringes with respect to a reference lattice here chosen as the substrate. GPA thus allows the local strain present in the different layers to be revealed: in-plane strain  $\epsilon_{yy} = \frac{\partial u_y}{\partial y}$  (along [010]<sub>pc</sub>, i.e., perpendicular to the growth direction), out-of-plane strain  $\epsilon_{zz} = \frac{\partial u_z}{\partial z}$  (along [001]<sub>pc</sub> i.e., along the growth direction), shear strain  $\epsilon_{yz} = \frac{1}{2} \left( \frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial z} \right)$ , and rotation  $\omega_{yz} = \frac{1}{2} \left( \frac{\partial u_x}{\partial y} - \frac{\partial u_y}{\partial z} \right)$ . This is particularly useful for the



study of the domain configuration in  $\text{PbTiO}_3$ , as the polarization is related to the strain from the strong strain-polarization coupling.<sup>51</sup> At room temperature,  $\text{PbTiO}_3$  is tetragonal with the polarization pointing along the long tetragonal axis. The strain orientation and amplitude, therefore, indicate the orientation and magnitude of the polarization.

We determine the periodicity of the superstructures in the  $\text{PbTiO}_3$  and  $\text{SrRuO}_3$  layers by measuring the distances between the additional reciprocal space spots obtained after FFT. The accuracy of the measurement was estimated by considering the diffraction spot extension as the lower and upper limits for the superstructure length estimation.

#### D. X-ray diffraction

In-house XRD measurements were performed using a *Panalytical X'Pert* diffractometer with  $\text{Cu K}\alpha_1$  radiation ( $1.540\,598\,0\text{ \AA}$ ) equipped with a 2-bounce  $\text{Ge}(220)$  monochromator and a triple axis detector. The  $\theta$ - $2\theta$  scans were analyzed using the *InteractiveXRDfit* software.<sup>52</sup> This XRD system is also equipped with a PIXcel 1D detector, used for faster acquisition of reciprocal space maps.

#### SUPPLEMENTARY MATERIAL

supplementary material contains a detailed description of the orthorhombic orientations, with a schematic diagram showing the pseudocubic representation of the  $(110)_o$ -oriented  $\text{DyScO}_3$  substrate and the six possible orthorhombic orientations of the  $\text{SrRuO}_3$  on the substrate; reciprocal space maps showing the high crystalline quality of the samples studied here and demonstrating the periodic pattern of the  $\text{PbTiO}_3$  layers; a table summarizing the different periods; and a discussion about the twin boundary observed in the  $\text{SrRuO}_3$  layer above the 45 u.c. thick  $\text{PbTiO}_3$  layer. Figure S2 showing the six possible orthorhombic orientations of  $\text{SrRuO}_3$  on  $(110)_o$ -oriented  $\text{DyScO}_3$  substrate can be found in high resolution here.

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#### IX AUTHOR DECLARATIONS

##### Conflict of Interest

The authors have no conflicts to disclose.

#### Author Contributions

C.L., M.H., A.G., and J.-M.T. designed the experiment. C.L., M.H., and L.T. grew the samples and conducted the AFM and XRD measurements and analysis. C.-P.S. and A.G. conducted the STEM measurements. I.G., C.-P.S., and A.G. performed advanced STEM analysis. C.L. wrote the manuscript with contributions from all authors. All authors discussed the experimental results and models, commented on the manuscript, and agreed on its final version.

**Céline Lichtensteiger:** Conceptualization (equal); Data curation (equal); Formal analysis (equal); Funding acquisition (equal); Investigation (equal); Methodology (equal); Project administration (equal); Resources (equal); Software (equal); Supervision (equal); Validation (equal); Visualization (equal); Writing – original draft (equal); Writing – review & editing (equal). **Chia-Ping Su:** Data curation (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Resources (equal); Software (equal); Writing – original draft (equal); Writing – review & editing (equal). **Iaroslav Gaponenko:** Data curation (equal); Formal analysis (equal); Investigation (equal); Software (equal); Validation (equal); Visualization (equal); Writing – original draft (equal); Writing – review & editing (equal). **Marios Hadjimichael:** Data curation (equal); Investigation (equal); Methodology (equal); Validation (equal); Writing – original draft (equal); Writing – review & editing (equal). **Ludovica Tovaglieri:** Data curation (equal); Formal analysis (equal); Investigation (equal); Writing – original draft (equal); Writing – review & editing (equal). **Patrycja Paruch:** Conceptualization (equal); Funding acquisition (equal); Writing – original draft (equal); Writing – review & editing (equal). **Alexandre Gloter:** Conceptualization (equal); Funding acquisition (equal); Supervision (equal); Writing – original draft (equal); Writing – review & editing (equal). **Jean-Marc Triscone:** Conceptualization (equal); Funding acquisition (equal); Supervision (equal); Writing – review & editing (equal).

#### DATA AVAILABILITY

The data that support the findings of this study are available in Yareta at <https://doi.org/10.26037/yareta:nt2pqmrilrc77nqy2yzjwdgtdu>.

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